|  | Concrete | Pictorial | Abstract |
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| Understanding numbers to 10,000 | Use place value equipment to understand the place value of 4-digit numbers. <br> thousands equal 4,000. <br> thousand is 10 hundreds. | Represent numbers using place value counters once children understand the relationship between 1,000s and 100s. $000+500+40+2=2,542$ | Understand partitioning of 4-digit numbers, including numbers with digits of 0 . $000+60+8=5,068$ <br> Understand and read 4-digit numbers on a number line. |
| Choosing mental methods where appropriate | Use unitising and known facts to support mental calculations. <br> Make 1,405 from place value equipment. <br> Add 2,000. <br> Now add the 1,000s. <br> 1 thousand +2 thousands $=3$ thousands $1,405+2,000=3,405$ | Use unitising and known facts to support mental calculations. <br> I can add the 100s mentally. $200+300=500$ | Use unitising and known facts to support mental calculations. $\begin{aligned} & 4,256+300=? \\ & 2+3=5 \quad 200+300=500 \\ & 4,256+300=4,556 \end{aligned}$ |



|  |  |  | Include examples that exchange in more than one column. |
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| Representing additions and checking strategies |  | Bar models may be used to represent additions in problem contexts, and to justify mental methods where appropriate. <br> I chose to work out $574+800$, then subtract 1. <br> This is equivalent to $3,000+3,000$. | Use rounding and estimating on a number line to check the reasonableness of an addition. $912+6,149=?$ <br> I used rounding to work out that the answer should be approximately $1,000+6,000=7,000 .$ |
| Year 4 <br> Subtraction |  |  |  |
| Choosing mental methods where appropriate | Use place value equipment to justify mental methods. | Use place value grids to support mental methods where appropriate. $7,646-40=7,606$ | Use knowledge of place value and unitising to subtract mentally where appropriate. $501-2,000$ <br> thousands -2 thousands $=1$ thousand $501-2,000=1,501$ |


|  | What number will be left if we take away 300? |  |  |
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| Column subtraction with exchange | Understand why exchange of a 1,000 for 100 s , a 100 for 10 s, or a 10 for 1 s may be necessary. | Represent place value equipment on a place value grid to subtract, including exchanges where needed. | Use column subtraction, with understanding of the place value of any exchange required. |
| Column <br> subtraction with exchange across more than one column | Understand why two exchanges may be necessary. $2,502-243=?$ | Make exchanges across more than one column where there is a zero as a place holder. $2,502-243=?$ | Make exchanges across more than one column where there is a zero as a place holder. $2,502-243=?$ |


|  | g <br> I need to exchange a 10 for some 1 s , but there are not any 10 s here. |  | $\begin{array}{rrrr} \text { Th } & \mathrm{H} & \mathrm{~T} & \mathrm{O} \\ \hline 2 & 48 & \mathrm{C}^{\prime} \varnothing & 12 \\ - & 2 & 4 & 3 \\ \hline 2 & 2 & 5 & 9 \\ \hline \end{array}$ |
| :---: | :---: | :---: | :---: |
| Representing subtractions and checking strategies |  | Use bar models to represent subtractions where a part needs to be calculated. <br> I can work out the total number of Yes votes using 5,762-2,899. <br> Bar models can also represent 'find the difference' as a subtraction problem. | Use inverse operations to check subtractions. <br> I calculated 1,225-799=574. <br> I will check by adding the parts. <br> The parts do not add to make 1,225. I must have made a mistake. |


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| Year 4 Multiplication |  |  |  |
| Multiplying by multiples of 10 and 100 | Use unitising and place value equipment to understand how to multiply by multiples of 1 , 10 and 100. <br> 3 groups of 4 ones is 12 ones. <br> 3 groups of 4 tens is 12 tens. <br> 3 groups of 4 hundreds is 12 hundreds. | Use unitising and place value equipment to understand how to multiply by multiples of 1 , 10 and 100. $\begin{aligned} & 3 \times 4=12 \\ & 3 \times 40=120 \\ & 3 \times 400=1,200 \end{aligned}$ | Use known facts and understanding of place value and commutativity to multiply mentally. $\begin{aligned} & 4 \times 7=28 \\ & 4 \times 70=280 \\ & 40 \times 7=280 \end{aligned}$ $\begin{aligned} & 4 \times 700=2,800 \\ & 400 \times 7=2,800 \end{aligned}$ |
| Understanding times-tables up to $12 \times 12$ | Understand the special cases of multiplying by 1 and 0. $\times 1=5$ $5 \times 0=0$ | Represent the relationship between the $\times 9$ table and the $\times 10$ table. <br> Represent the $\times 11$ table and $\times 12$ tables in relation to the $\times 10$ table. $\times 11=20+2$ | Understand how times-tables relate to counting patterns. <br> Understand links between the $\times 3$ table, $\times 6$ table and $\times 9$ table $5 \times 6$ is double $5 \times 3$ <br> $\times 5$ table and $\times 6$ table <br> I know that $7 \times 5=35$ <br> so I know that $7 \times 6=35+7$. <br> $\times 5$ table and $\times 7$ table $3 \times 7=3 \times 5+3 \times 2$ |


|  |  | $\begin{aligned} & \times 11=30+3 \\ & \times 11=40+4 \\ & \\ & \times 12=40+8 \end{aligned}$ | $\times 9$ table and $\times 10$ table $\begin{aligned} & 6 \times 10=60 \\ & 6 \times 9=60-6 \end{aligned}$ |
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| Understanding and using partitioning in multiplication | Make multiplications by partitioning. <br> $4 \times 12$ is 4 groups of 10 and 4 groups of 2 . $4 \times 12=40+8$ | Understand how multiplication and partitioning are related through addition. | Use partitioning to multiply 2-digit numbers by a single digit. $8 \times 6=?$ $\begin{aligned} 18 \times 6 & =\underbrace{10 \times 6}_{1}+\underbrace{8 \times 6}_{1} \\ & =60+48 \\ & =108 \end{aligned}$ $\begin{aligned} 8 \times 6 & =10 \times 6+8 \times 6 \\ & =60+48 \\ & =108 \end{aligned}$ |
| Column multiplication for 2- and 3-digit numbers multiplied by a single digit | Use place value equipment to make multiplications. <br> 1ake $4 \times 136$ using equipment. <br> I can work out how many 1s, 10s and 100s. | Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit. | Use the formal column method for up to 3-digit numbers multiplied by a single digit. $\begin{array}{r} 312 \\ \times \quad 3 \\ \hline 936 \\ \hline \end{array}$ <br> Understand how the expanded column method is related to the formal column method and |


|  | There are $4 \times 6$ ones... 24 ones <br> There are $4 \times 3$ tens ... 12 tens <br> There are $4 \times 1$ hundreds ... 4 hundreds $24+120+400=544$ |  | understand how any exchanges are related to place value at each stage of the calculation. |
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| Multiplying more than two numbers | Represent situations by multiplying three numbers together. <br> Each sheet has $2 \times 5$ stickers. <br> There are 3 sheets. <br> There are $5 \times 2 \times 3$ stickers in total. $\begin{aligned} & \underbrace{5 \times 2}_{10 \times 3} \times 3=30 \\ & 10 \times 30 \end{aligned}$ | Understand that commutativity can be used to multiply in different orders. | Use knowledge of factors to simplify some multiplications. $\left\{\begin{array}{c} 4 \times 5=12 \times 2 \times 5 \\ 12 \times 2 \times 5= \\ 12 \times 10=120 \end{array}\right.$ <br> So, $24 \times 5=120$ |
| Year 4 <br> Division |  |  |  |
| Understanding the relationship between multiplication | Use objects to explore families of multiplication and division facts. | Represent divisions using an array. | Understand families of related multiplication and division facts. <br> know that $5 \times 7=35$ |


| and division, including times-tables | $4 \times 6=24$ <br> 24 is 6 groups of 4 . <br> 24 is 4 groups of 6 . <br> 24 divided by 6 is 4 . <br> 24 divided by 4 is 6 . | $28 \div 7=4$ | $\begin{aligned} & \text { I know all these facts: } \\ & \times 7=35 \\ & \times 5=35 \\ & 5=5 \times 7 \\ & 5=7 \times 5 \\ & 5 \div 5=7 \\ & 5 \div 7=5 \\ & =35 \div 5 \\ & =35 \div 7 \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| Dividing multiples of 10 and 100 by a single digit | Use place value equipment to understand how to use unitising to divide. <br> 8 ones divided into 2 equal groups 4 ones in each group <br> 8 tens divided into 2 equal groups 4 tens in each group <br> 8 hundreds divided into 2 equal groups 4 hundreds in each group | Represent divisions using place value equipment. $9 \div 3=3$ <br> 9 tens divided by 3 is 3 tens. <br> 9 hundreds divided by 3 is 3 hundreds. | Use known facts to divide 10s and 100s by a single digit. $\begin{aligned} & 5 \div 3=5 \\ & 50 \div 3=50 \\ & 500 \div 3=500 \end{aligned}$ |
| Dividing 2-digit and 3-digit numbers by a | Partition into 10 s and 1 s to divide where appropriate. | Partition into $100 \mathrm{~s}, 10$ s and 1 s using Base 10 equipment to divide where appropriate. | Partition into $100 \mathrm{~s}, 10 \mathrm{~s}$ and 1 s using a part-whole model to divide where appropriate. |


| single digit by partitioning into 100s, 10s and 1s | $39 \div 3=?$ $\begin{gathered} 39=30+9 \\ \\ 30 \div 3=10 \\ 9 \div 3=3 \\ 39 \div 3=13 \end{gathered}$ | $39 \div 3=?$ <br> 3 groups of I ten <br> 3 groups of 3 ones $39=30+9$ $\begin{gathered} 30 \div 3=10 \\ 9 \div 3=3 \\ 39 \div 3=13 \end{gathered}$ | $42 \div 2=?$ $\left\{\begin{array}{c} p o \div 2=50 \\ 40 \div 2=20 \\ 6 \div 2=3 \\ p+20+3=73 \\ 142 \div 2=73 \end{array}\right.$ |
| :---: | :---: | :---: | :---: |
| Dividing 2-digit and 3-digit numbers by a single digit, using flexible partitioning | Use place value equipment to explore why different partitions are needed. $2 \div 3=?$ <br> I will split it into 30 and 12, so that I can divide by 3 more easily. | Represent how to partition flexibly where needed. $4 \div 7=?$ <br> will partition into 70 and 14 because I am dividing by 7. <br> $84 \div 7=12$ | Make decisions about appropriate partitioning based on the division required. <br> Understand that different partitions can be used to complete the same division. <br> $30 \div 3=10 \quad 30 \div 3=10 \quad 30 \div 3=10 \quad 30 \div 3=10 \quad 12 \div 3=4$ |


| Understanding remainders | Use place value equipment to find remainders. 5 shared into 4 equal groups here are 24 , and 1 that cannot be shared. $\square$ $\square$ <br> $\square$ $\square$ $\square$ | Represent the remainder as the part that cannot be shared equally. <br> $2 \div 5=14$ remainder 2 | Understand how partitioning can reveal remainders of divisions. $\begin{aligned} & b \div 4=20 \\ & z \div 4=3 \end{aligned}$ <br> $5 \div 4=23$ remainder 3 |
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