

Concrete				Pictorial	Abstract			
Year 6 Addition								
Comparing and selecting efficient methods	Represent grid, and u mental me	ise th	is to s	•		0	Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation. Compare written and mental methods alongside place value representations.	Use column addition where mental methods are not efficient. Recognise common errors wit column addition. 32,145 + 4,302 = ?
			9				$\frac{1}{40.265}$ $\frac{1}{43.265}$ $\frac{1}{40.265}$ $\frac{1}{43.265}$ $\frac{1}{40.265}$ $\frac{1}{40.265}$ $\frac{1}{40.265}$ $\frac{1}{40.265}$ $\frac{1}{40.265}$ $\frac{1}{40.265}$ $\frac{1}{40.265}$ $\frac{1}{40.265}$ $\frac{1}{35.22}$ $\frac{1}{35.22}$ Use bar model and number line representations to model addition in problem-solving and measure contexts. $\frac{1}{1000}$ $\frac{1}{12:05}$ $\frac{1}{13:05}$ $\frac{1}{13:13}$	$\frac{\text{TTh Th H T O}}{3 2 1 4 5}$ $+ \frac{4 3 0 2}{3 6 4 4 7}$ $+ \frac{4 3 0 2}{7 5 1 6}$ $\frac{\text{TTh Th H T}}{3 2 1 4}$ $+ \frac{4 3 0 2}{7 5 1 6}$ $\frac{\text{Which method has been completed accurately?}}{\text{What mistake has been made?}}$ Column methods are also used for decimal additions where mental methods are not efficient.} $\frac{\text{H T O Tth Hth}}{1 4 0 \cdot 0 9}$ $+ \frac{4 9 \cdot 8 9}{1 8 9 \cdot 9 8}$

Selecting mental methods for larger numbers where appropriate	Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods. $\underbrace{\hline M  HTh  TTh  Th  H  T  O}_{\bullet \bullet $	Use a bar model to support thinking in addition problems. 257,000 + 99,000 = ? fill = 100,000 I added 100 thousands then subtracted 1 thousand. 257 thousands + 100 thousands = 357 thousands 257,000 + 100,000 = 357,000 357,000 - 1,000 = 356,000 So, 257,000 + 99,000 = 356,000	Use place value and unitising to support mental calculations with larger numbers. 195,000 + 6,000 = ? 195 + 5 + 1 = 201 195 thousands + 6 thousands = 201 thousands So, 195,000 + 6,000 = 201,000		
Understanding order of operations in calculations	Use equipment to model different interpretations of a calculation with more than one operation. Explore different results. $3 \times 5 - 2 = ?$	Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations. $16 \times 4$ cab $444444444444444444444444444444444444$	Understand the correct order of operations in calculations without brackets. Understand how brackets affect the order of operations in a calculation. $4 + 6 \times 16$ 4 + 96 = 100 $(4 + 6) \times 16$ $10 \times 16 = 160$		

	$3 \times 5 - 2$ $\downarrow \qquad \qquad$		
Year 6 Subtraction			
Comparing and selecting efficient methods	Use counters on a place value grid to represent subtractions of larger numbers.	Compare subtraction methods alongside place value representations. $\begin{array}{r} \hline +4 & -30 & -500 \\ \hline +2,  45 & 2,  49 & 2,  79 & 2, 679 \end{array}$ $\hline \hline 1 & H & T & 0 \\ \hline 2 & 6 & 7 & 9 \\ \hline - & 5 & 3 & 4 \\ \hline 2 & 1 & 4 & 5 \end{array}$ Use a bar model to represent calculations, including 'find the difference' with two bars as comparison. $\hline computer game \\ \hline puzzle book & fl2.50 \end{array}$	Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy. $\frac{\frac{Th}{1} + \frac{H}{3} + \frac{T}{9} + \frac{O}{12}}{\frac{-15}{3} + \frac{6}{1,552} + \frac{-400}{1,552} + \frac{6}{1,552} + \frac{-400}{1,552}}$ Use column subtraction for decimal problems, including in the context of measure. $\frac{H}{3} + \frac{T}{9} + \frac{O}{6} + \frac{T}{10} + \frac{O}{1} + \frac{1}{10} + \frac{O}{10} + \frac{O}{1$

Subtracting mentally with larger numbers		Use a bar model to show how unitising can support mental calculations. 950,000 - 150,000 That is 950 thousands - 150 thousands $950 \leftrightarrow 800$ So, the difference is 800 thousands. 950,000 - 150,000 = 800,000	Subtract efficiently from powers of 10. 10,000 – 500 = ?
Year 6 Multiplication			
Multiplying up to a 4-digit number by a single digit number	Use equipment to explore multiplications. Th H T O OOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOO	Use place value equipment to compare methods. Method I $3 \ 2 \ 2 \ 5$ $3 \ 2 \ 2 \ 5$ $1 \ 2 \ 9 \ 0 \ 0$ $1 \ 2 \ 9 \ 0 \ 0$ Method 2 Method 2 $4 \times 3,000 \ 4 \times 200 \ 4 \times 20 \ 4 \times 5$ $12,000 \ + \ 800 \ + \ 80 \ + \ 20 = 12,900$	Understand area model and short multiplication. Compare and select appropriate methods for specific multiplications. Method 3 $3.000 \ 200 \ 20 \ 5 \\ 4 \ 12,000 \ 800 \ 80 \ 20 \\ 12.000 + 800 + 80 + 20 = 12,900 \\ \\ Method 4 \\ 3 \ 2 \ 2 \ 5 \\ \times \ 4 \ 1 \ 2 \ 9 \ 0 \ 0 \\ 1 \ 2 \ 9 \ 0 \ 0 \\ \hline \ 1 \ 2 \ 9 \ 0 \ 0 \\ \hline \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
Multiplying up to a 4-digit number by a 2-digit number		Use an area model alongside written multiplication.	Use compact column multiplication with understanding of place value at all stages.

		Mathead	
		Method I	I 2 3 5 × 2 I
		1,000 200 30 5	× I 2 3 5 I × I,235
		20 20,000 4,000 600 100	2 4 7 0 0 20 × 1,235
		I I,000 200 30 5	2 5 9 3 5 21 × 1,235
		1 2 3 5	
		× 21	
		5 l×5	
		3 0 I×30	
		2 0 0 I × 200 I 0 0 0 I × 1,000	
		1 0 0 20×5	
		6 0 0 20×30	
		4 0 0 0 20×200 2 0 0 0 0 20×1,000	
		2 5 9 3 5 21 × 1,235	
Using knowledge	Use equipment to understand square numbers	Compare methods visually using an area model.	Use a known fact to generate families of related
of factors and	and cube numbers.	Understand that multiple approaches will	facts.
partitions to		produce the same answer if completed	
compare		accurately.	
methods for		5300 5000 300	
multiplications		5,200 5,000 200 20 5,200 × 20 25 5,000 × 25 200 × 25	
		5 <u>5,200 × 5</u> (5,200 × 25)	I,870 ÷ II = I70
	a fair		
		5,000 200 5.200	
	$5 \times 5 = 5^2 = 25$	20 5,000 × 20 200 × 20 5,200 × 25	170 × 12 17 × 110
	$5 \times 5 \times 5 = 5^3 = 25 \times 5 = 125$	5 5.000 × 5 200 × 5	
		5,200	
		5 5,200 × 5 5,200 × 5 100	Use factors to calculate efficiently.
		5 5,200 × 5	
		5 5,200 × 5 5 5 5,200 × 5	15 × 16
			= 3 × 5 × 2 × 8
			= 3 × 8 × 2 × 5
		Represent and compare methods using a bar	= 24 × 10
		model.	= 240

1,000	in decimal multiplication.	numbers on a place value grid.	Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000. $8 \times 100 = 800$			
	Represent 0-3.		$8 \times 100 = 800$ $8 \times 300 = 800 \times 3$ = 2,400 $2.5 \times 10 = 25$ $2.5 \times 20 = 2.5 \times 10 \times 2$ = 50			
	$0.3 \times 10 = ?$ 0.3 is 3 tenths. $10 \times 3$ tenths are 30 tenths. 30 tenths are equivalent to 3 ones.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				
Multiplying decimals	Explore decimal multiplications using place value equipment and in the context of measures.	Represent calculations on a place value grid. $3 \times 3 = 9$ $3 \times 0.3 = 0.9$ TOOTTH 0000 0000 Understand the link between multiplying decimals and repeated addition. TOOTHOUSE +0.2 +0.2 +0.2 +0.2 +0.2 +0.2 +0.2 +0.2	Use known facts to multiply decimals. x = 3 = 12 x = 0.3 = 1.2 x = 0.03 = 0.12 $0 \times 5 = 100$ $0 \times 0.5 = 10$ $0 \times 0.05 = 1$ Find families of facts from a known multiplication. know that $18 \times 4 = 72$ . his can help me work out: $8 \times 4 = ?$			

	$4 \times 0.3 \text{ cm} = 1.2 \text{ cm}$ $4 \times 1.3 = 4 + 1.2 = 5.2$	ст					8 × 0·4 = ? 80 × 0·4 = 8 × 0·04 = Use a pla of multip	? ? ce valu	-		nders	stand	the effe	ects
							2 × 3	H	Т	0 6	•	Tth	Hth	
							0·2 × 3			0	•	6		
							0·02 × 3				•			
Year 6 Division														
Understanding factors	Use equipment to exp number.	lore different factors of a	Recognise prime exactly two fact division and rem	ors. Understa		-	Recognis Understa that 1 is i	nd tha	at 2 is t	the or	ily ev			ıd
	$24 \div 4 = 6$	30 ÷ 4 = 7 remainder 2						<ol> <li>3 4</li> <li>13 14</li> <li>23 24</li> </ol>		6 (17)	18 (	9 10 9 20 29 30		
	$24 \div 4 = 6$ 4 is a factor of 24 but		17 ÷ 2 = 8 r I	17 ÷ 3 = 5 r 2	17 ÷ 4 = 4 r I	17 ÷ 5 = 3 r 2	3] 32	<ul> <li>23 24</li> <li>33 34</li> <li>43 44</li> </ul>	35 3	6 37	38 3	-		

Dividing by a single digit	Use equipment to make groups from a total.	H       T       O         O       O       O       O         O       O       O       O       O       O         H       T       O       O       O       O       O       O       O       O       O       O       O       O       O       O       O       O       O       O	Use short division to divide by a single digit. $ \begin{array}{c} 0\\ 6 \overline{)1}^{1}3 2\\ \end{array} $ $ \begin{array}{c} 0\\ 2\\ 6 \overline{)1}^{2}3 2\\ \end{array} $ $ \begin{array}{c} 0\\ 2\\ 6 \overline{)1}^{2}3 2\\ \end{array} $ $ \begin{array}{c} 0\\ 2\\ 6 \overline{)1}^{2}2\\ \end{array} $ Use an area model to link multiplication and division. $ \begin{array}{c} 7\\ 6 \overline{)132}\\ 6 \overline{)60} 6\\ 6 \overline{)60} 6\\ \end{array} $ $ \begin{array}{c} 10\\ 10\\ 11\\ 6\\ 6 \overline{)60} 6\\ 6\\ 6\\ 120\\ 12\\ 132 = 120 + 12\\ 132 \div 6 = 20 + 2 = 22\end{array} $
Dividing by a 2-digit number using factors	Understand that division by factors can be used when dividing by a number that is not prime.	Use factors and repeated division. $1,260 \div 14 = ?$ $1,260 \div 2 = 630$ $630 \div 7 = 90$ $1,260 \div 14 = 90$	Use factors and repeated division where appropriate. 2,100 ÷ 12 = ? $2,100 \rightarrow (+2) \rightarrow (+6) \rightarrow (+2) \rightarrow (+6) \rightarrow (+2) \rightarrow (+6) \rightarrow (+2) \rightarrow (+6) \rightarrow (+2) \rightarrow$

Dividing by a 2-digit number using long division	Use equipment to build numbers from groups. 182 divided into groups of 13. There are 14 groups.	Use an area model alongside written division to model the process. $377 \div 13 = ?$ 7 13 $37710$ $?13$ $30$ $24713$ $10$ $?13$ $10$ $?13$ $10$ $?13$ $10$ $?13$ $10$ $1713$ $10$ $1713$ $10$ $1713$ $13$ $13$ $17377 \div 13 = 29$	Use long division where factors are not useful (for example, when dividing by a 2-digit prime number). Write the required multiples to support the division process. $377 \div 13 = ?$ $\begin{array}{r} & & & & & & & & & & & & & & & & & & &$
			division completed above rather than at the side.

			$3$ $21 \overline{7 \ 9 \ 8}$ $- \frac{6}{6} \frac{3}{3} \frac{0}{1}$ $21 \overline{7 \ 9 \ 8}$ $- \frac{3}{6} \frac{3}{3} \frac{0}{1}$ $- \frac{6}{1} \frac{3}{6} \frac{0}{8}$ $- \frac{1}{6} \frac{6}{8} \frac{0}{0}$ Divisions with a remainder explored in problem-solving contexts.
Dividing by 10, 100 and 1,000	Use place value equipment to explore division as exchange. $\overbrace{\begin{array}{c} \bullet \bullet$	Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid. $\begin{array}{c c c c c c c c c c c c c c c } & \hline & $	Use knowledge of factors to divide by multiples of 10, 100 and 1,000. $40 \div 50 = 10$ $40 \rightarrow \div 10 \rightarrow \div 5 \rightarrow ?$ $40 \rightarrow \div 5 \rightarrow \div 10 \rightarrow ?$ $40 \div 5 = 8$ $8 \div 10 = 0.8$ $So, 40 \div 50 = 0.8$
Dividing decimals	Use place value equipment to explore division of decimals.	Use a bar model to represent divisions.	Use short division to divide decimals with up to 2 decimal places.

8 tenths divided into 4 groups. 2 tenths in each group.	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
		$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$